

Yr 11/12

**RSHS SCHOOL**

yr 11/12 sems 2 Examination, 2012

Question/Answer Booklet

**MATHEMATICS 3A/3B**

Section One:  
Calculator-free

**SOLUTIONS**

Student Number: In figures

--	--	--	--	--	--	--	--

In words

Your name

MARKING KEY

**Time allowed for this section**

Reading time before commencing work: five minutes

Working time for this section: fifty minutes

**Materials required/recommended for this section**

*To be provided by the supervisor*

This Question/Answer Booklet

Formula Sheet

*To be provided by the candidate*

Standard items: pens, pencils, pencil sharpener, eraser, correction fluid/tape, ruler, highlighters

Special items: nil

**Important note to candidates**

No other items may be used in this section of the examination. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

## Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of exam
Section One: Calculator-free	7	7	50	50	33
Section Two: Calculator-assumed	12	12	100	100	67
<b>Total</b>				150	100

## Instructions to candidates

- The rules for the conduct of Western Australian external examinations are detailed in the *Year 12 Information Handbook 2012*. Sitting this examination implies that you agree to abide by these rules.
- Write your answers in the spaces provided in this Question/Answer Booklet. Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
  - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
  - Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question(s) that you are continuing to answer at the top of the page.
- Show all your working clearly.** Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.
- It is recommended that you **do not use pencil**, except in diagrams.

**Section One: Calculator-free****(50 Marks)**

This section has **seven (7)** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time for this section is 50 minutes.

---

**Question 1****(3 marks)**

Find the values of  $x$  and  $y$  if  $3x + 2y = -4$  and  $5x - 3y = 25$ .

Eqn 1 times 3	$9x + 6y = -12$	✓
Eqn 2 times 2	$10x - 6y = 50$	✓
Add	$19x = 38$	
	$x = 2$	✓
	$y = -5$	

Question 2

(9 marks)

(a) If  $a = 5 \times 10^2$  and  $b = 8 \times 10^6$  evaluate  $a^2 \div b^{1/3}$ .

(3 marks)

$$\frac{5^2 \times 10^{2 \times 2}}{8^{1/3} \times (10^6)^{1/3}} = \frac{25 \times 10^4}{2 \times 10^2}$$

$$= 12.5 \times 10^2$$

$$= 1250$$

✓  
✓  
✓ Either form

(b) Solve the following for  $x$ .

(i)  $25^x = 125\sqrt{5}$

(3 marks)

$$5^{2x} = 5^3 \times 5^{0.5}$$

$$2x = 3.5$$

$$x = \frac{7}{4} \quad (1.75)$$

✓  
✓  
✓

(ii)  $\frac{(2x-3)^3}{4} = 16$

(3 marks)

$$(2x-3)^3 = 64$$

$$(2x-3)^3 = 4^3$$

$$2x-3 = 4$$

$$x = \frac{7}{2}$$

✓  
✓  
✓

## Question 3

(8 marks)

The universal set  $\{1, 2, 3, 4, 5, 6, 7\}$  has subsets  $A = \{1, 3, 5, 7\}$  and  $B = \{4, 5, 6\}$ .

(a) Determine  $n(\overline{A \cap B})$ .

(1 mark)

6



(b) List the elements of  $A \cup \overline{B}$ .

(2 marks)

{1, 2, 3, 5, 7}



(c) A four-digit PIN number is made by randomly choosing the first two digits from subset A and the last two digits from subset B. An example of such a PIN number is 3346.

(i) In how many ways can the first two digits be chosen?

(1 mark)

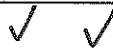
$4 \times 4 = 16$  ways



(ii) What is the probability that the last two digits chosen are both sixes?

(2 marks)

$$\frac{1 \times 1}{3 \times 3} = \frac{1}{9}$$



(iii) What is the probability that the PIN number starts with a five but does not end with a five?

(2 marks)

$$\frac{1 \times 4 \times 3 \times 2}{4 \times 4 \times 3 \times 3} = \frac{1}{6}$$



Question 4

(6 marks)

A set of test scores were 12, 9, 4, 16, 13, 2, 10, 11, 10, 15.

(a) State the mode of the scores.

(1 mark)

10 ✓

(b) The minimum and maximum scores are 2 and 16 respectively. Calculate the other statistics that would be required to construct a boxplot for these scores.

(3 marks)

2, 4, 9, 10, 10 (M) 11, 12, 13, 15, 16  
 Median is 10.5 ✓  
 Lower Quartile is 9 ✓  
 Upper Quartile is 13 ✓

(c) Use a calculation to decide whether or not the set of scores contains an outlier. (2 marks)

$IQR = 13 - 9 = 4$   
 $LQ - 1.5 \times IQR = 9 - 1.5 \times 4 = 3$   
 Any score below 3 is an outlier, so the score of 2 is an outlier - the set of scores **does** contain an outlier.

✓ Calculation  
 ✓

Question 5

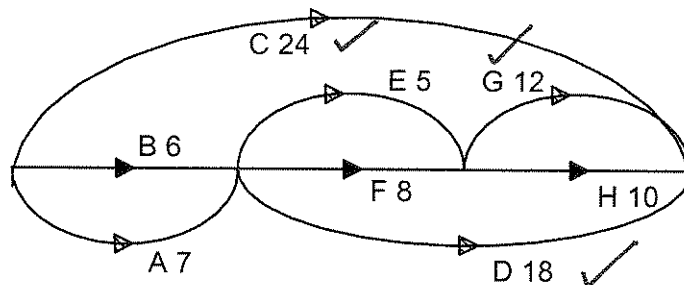
(8 marks)

The eight activities involved in a construction project, together with their completion times and immediate predecessors are shown in this table:

Activity	Time (days)	Immediate Predecessor
A	7	-
B	6	-
C	24	-
D	18	A, B
E	5	A, B
F	8	A, B
G	12	E, F
H	10	E, F

(a) Display this information as a project network.

(3 marks)



*Marks awarded for correct placement of tasks C, G & D as shown.*

(b) List the activities on the critical path and state the minimum completion time for this project.

(2 marks)

CP is A, F, G. ✓  
 MCT is  $7 + 8 + 12 = 27$  days ✓

*follow through*

(c) Consider each of the questions below in isolation.

(i) How many days can activity E be delayed, without an increase in the minimum completion time?

(1 mark)

3 days ✓

(ii) If the time taken by activity F is halved, what effect does this have on the minimum completion time and critical path?

(2 marks)

MCT decreases by 2 days to 25 days. ✓  
 New CP: A, D. ✓

Question 6

(9 marks)

(a)  $P = (t^2 - 2)(1 - 3t + 2t^2)$ .

Use the product rule to find  $\frac{dP}{dt}$ , simplifying your answer.

(4 marks)

$$\begin{aligned} \frac{dP}{dt} &= 2t(1 - 3t + 2t^2) + (t^2 - 2)(-3 + 4t) \\ &= 2t - 6t^2 + 4t^3 - 3t^2 + 4t^3 + 6 - 8t \\ &= 8t^3 - 9t^2 - 6t + 6 \end{aligned}$$

(b) A polynomial function  $f(x)$  passes through the point A(1, -2) and is such that  $f'(x) = 5 - 2x$ .

(i) Find the equation of the tangent to  $f(x)$  at the point A.

(2 marks)

$$\begin{aligned} f'(1) &= 5 - 2(1) \\ &= 3 \\ y - (-2) &= 3(x - 1) \\ y &= 3x - 5 \end{aligned}$$

(ii) Find  $f(x)$ .

(3 marks)

$$\begin{aligned} f(x) &= 5x - x^2 + c \\ -2 &= 5(1) - (1)^2 + c \\ c &= -6 \\ f(x) &= 5x - x^2 - 6 \end{aligned}$$



Question 7

(7 marks)

(a) Prove that the product of any two odd numbers will always be odd.

(4 marks)

Let the odd numbers be  $2n + 1$  and  $2m + 1$ . ✓

Then their product is

$$\begin{aligned} (2n + 1)(2m + 1) &= 4nm + 2n + 2m + 1 \\ &= 2(2nm + n + m) + 1 \end{aligned}$$

Hence the product is odd as it is of the form  $2p + 1$  ✓

(b) A simple polygon is a closed two-dimensional shape, made of straight lines and with only one boundary that doesn't cross over itself.

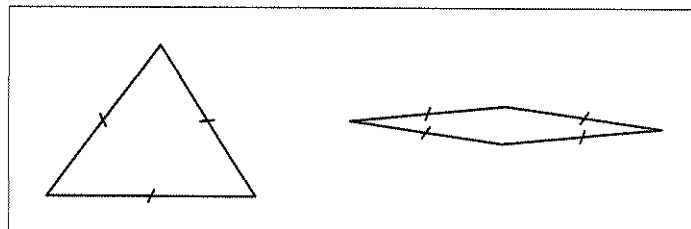
Consider the conjecture: "If all the sides are of length  $d$ , then as the number of sides of a polygon increases, so does the area of the polygon."

State whether the conjecture is true or false and justify your answer.

(3 marks)

Conjecture is false. ✓

A polygon must have 3 or more sides. A polygon with 3 equal length sides of  $d$  must be an equilateral triangle, as shown. The polygon shown with 4 equal length sides of  $d$  will obviously have a smaller area, showing that as the number of sides increases, the area does not.



✓✓ Reasoning and/or diagram

Additional working space

Question number: \_\_\_\_\_

Additional working space

Question number: \_\_\_\_\_

This examination paper may be freely copied, or communicated on an intranet, for non-commercial purposes within educational institutes that have purchased the paper from WA Examination Papers provided that WA Examination Papers is acknowledged as the copyright owner. Teachers within purchasing schools may change the paper provided that WA Examination Paper's moral rights are not infringed.

Copying or communication for any other purposes can only be done within the terms of the Copyright Act or with prior written permission of WA Examination papers.

*Published by WA Examination Papers  
PO Box 445 Claremont WA 6910*